



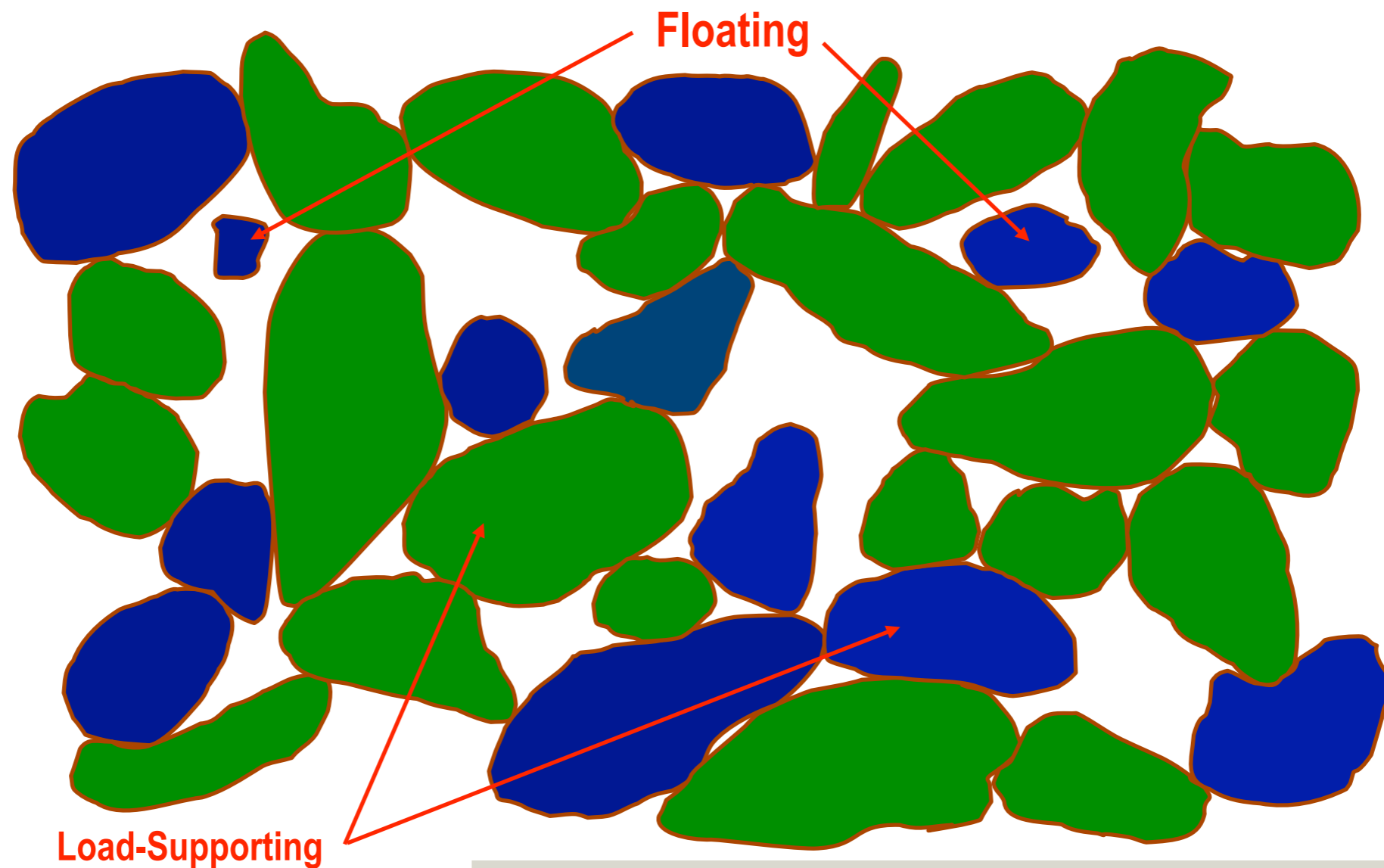
# Estimation of Permeability with Seismic “I really did mean to say permeability not porosity”

**Michael Glinsky**

# Outline

- rock physics model
- supporting measurements (log and core)
- numerical rock assembly model
- model based seismic inversion & practical detectability
- conclusions

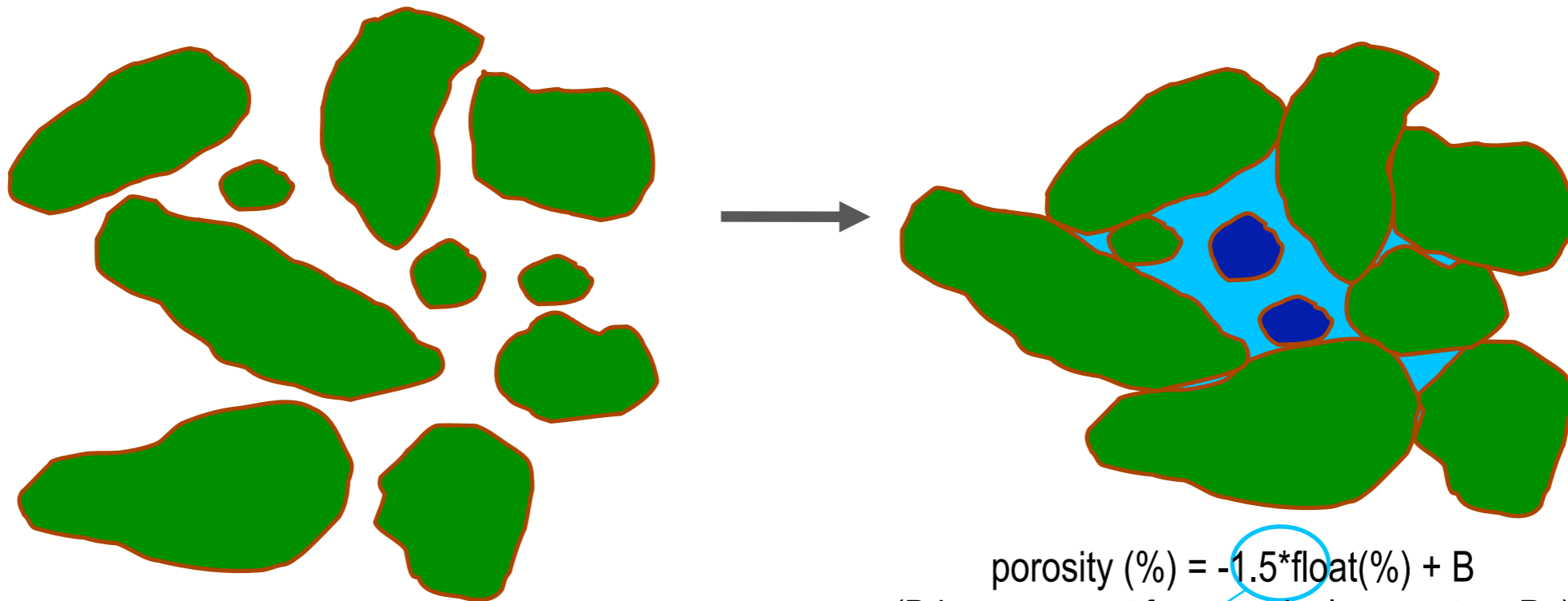
# Floating grain model - the link of deposition physics to grain scale properties, permeability



- Abundance of potential floating grains in the system is due to two factors
- overall abundance of silt/mud-sized particles (related to nature of clastic input and system-scale proximal vs distal position)
  - local variation due to depositional processes (e.g. rapid fallout vs traction)

# Capture ratio is another key concept

*At a constant Effective Stress - For every 3 small grains, 1 becomes part of matrix and 2 will float*



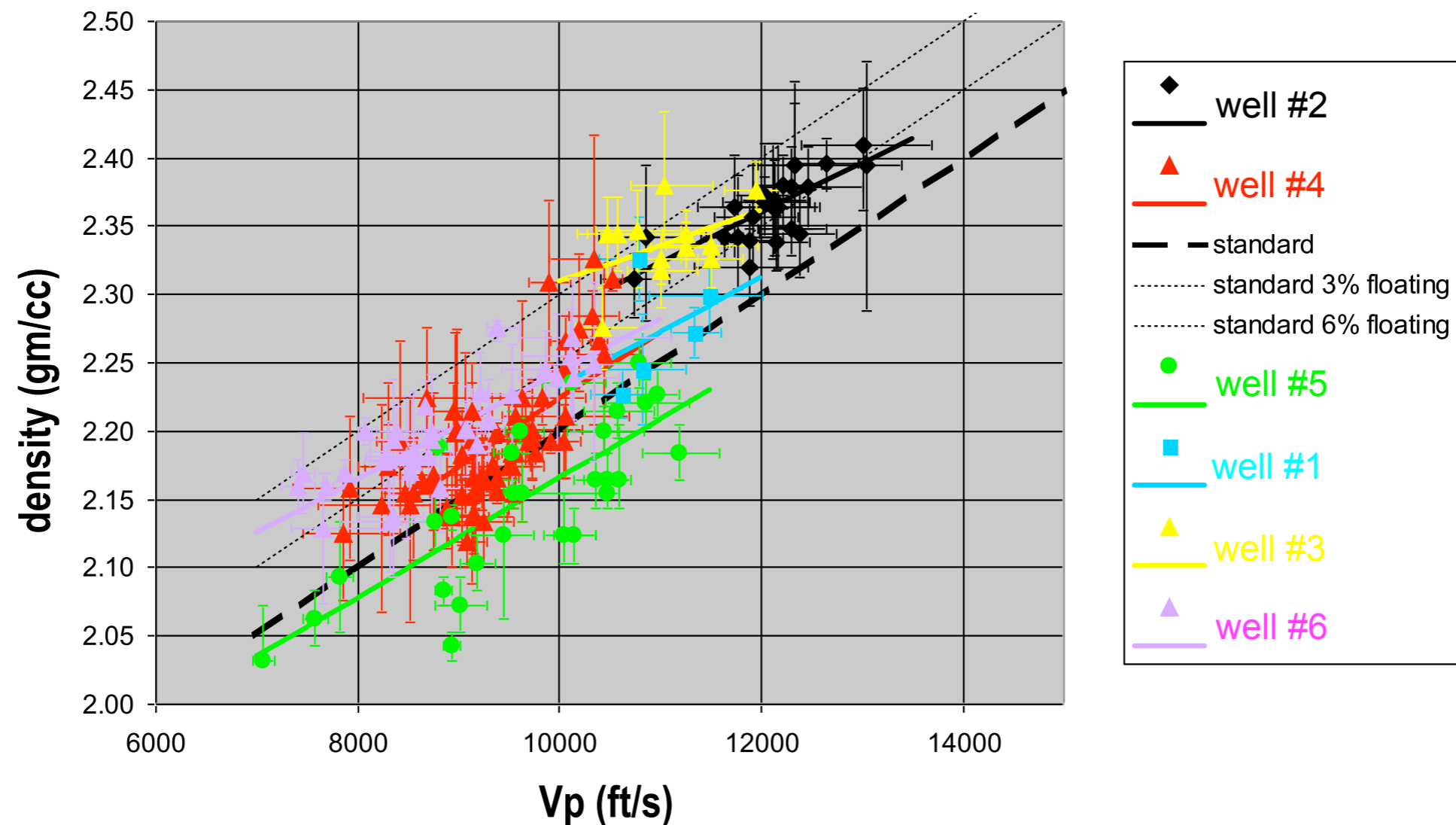
Bimodal grain sizes (big and small)

porosity (%) =  $-1.5 \cdot \text{float}(\%) + B$   
(B is a constant for a particular constant Pe)

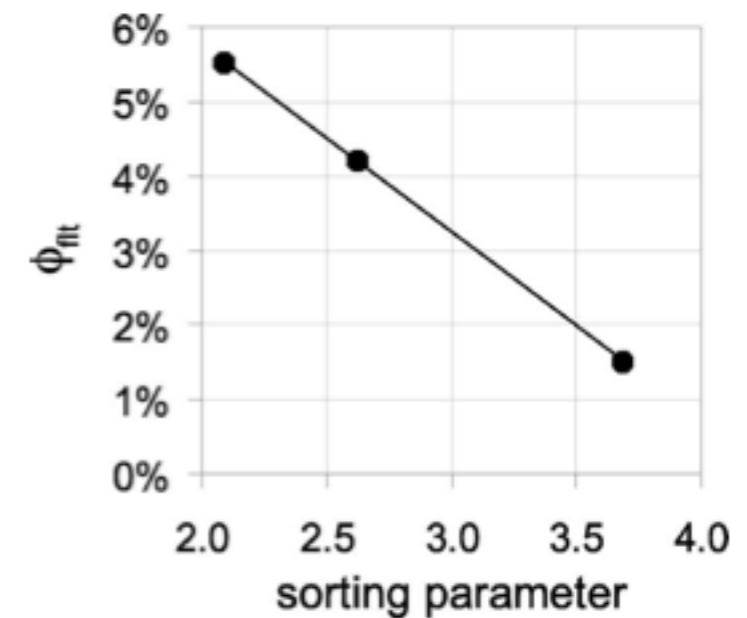
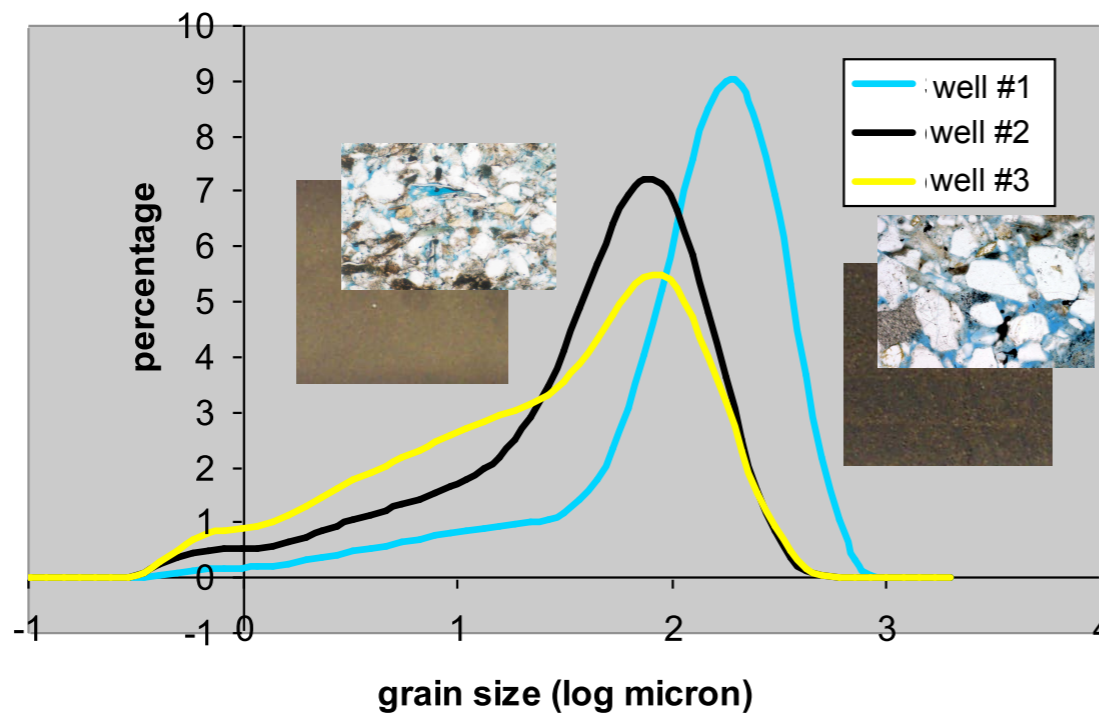
Capture Ratio =  $1 - (1/1.5) = 33\%$   
ie 1/3 of small grains are captured in to the load bearing matrix of the rock. The capture ratio will depend on the geometries of the original grains.

$$\text{porosity in \%} = -1.54 \cdot \text{float in \%} - 88\% \cdot (1 - \exp(-\text{Pe} / 800 \text{ psi})) + 110\% \quad \pm 0.2\%$$

# Petrophysical evidence for the floating grain model

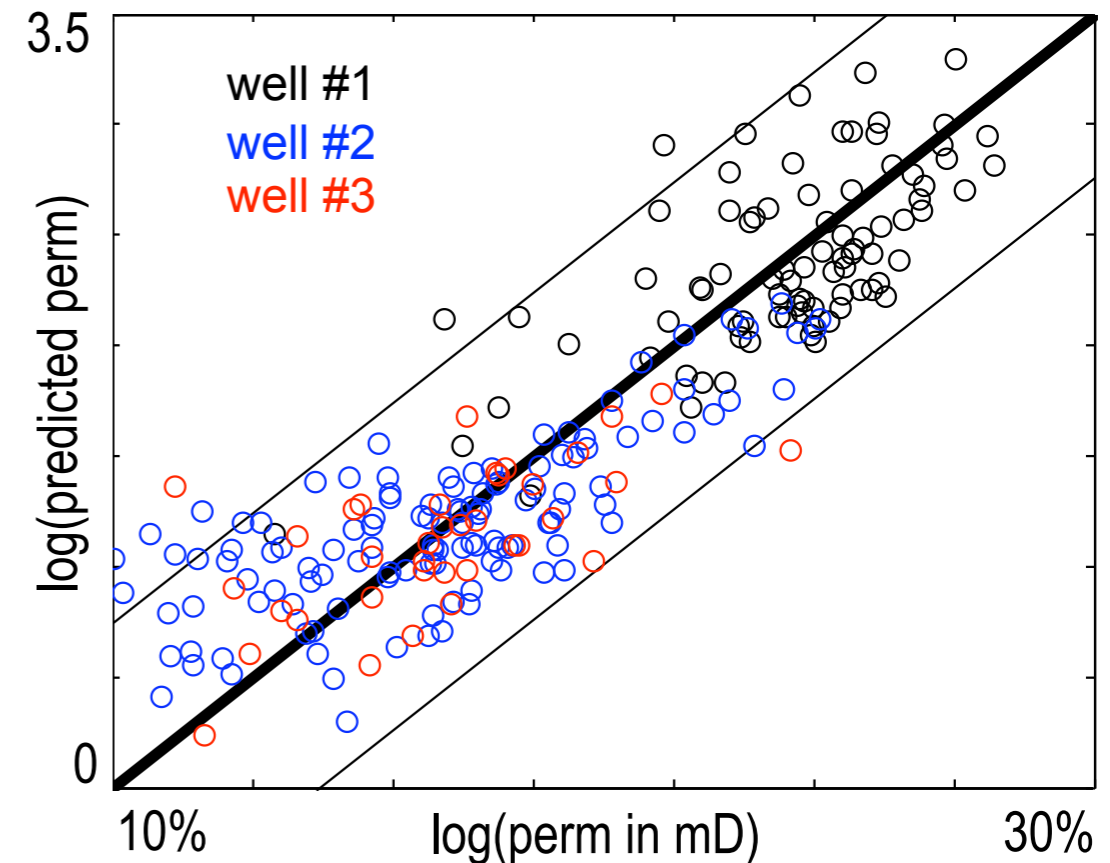
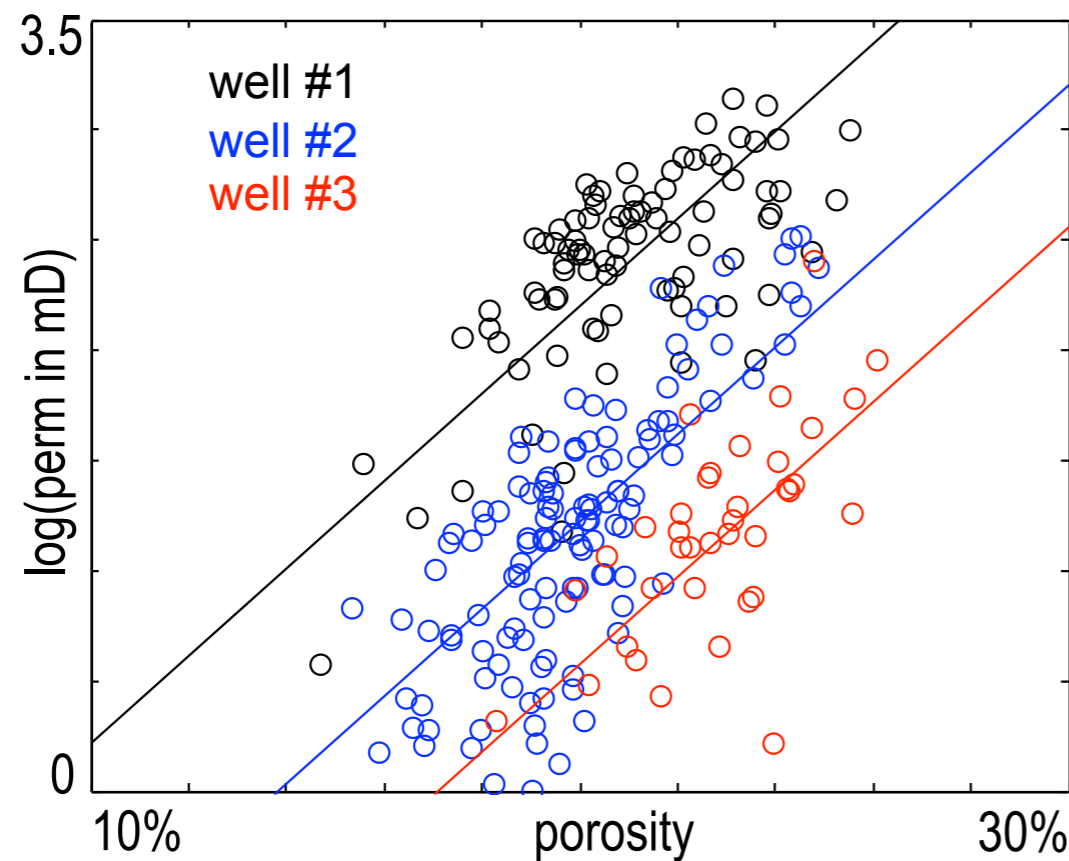


# Relationship between size distribution and floating grain fraction



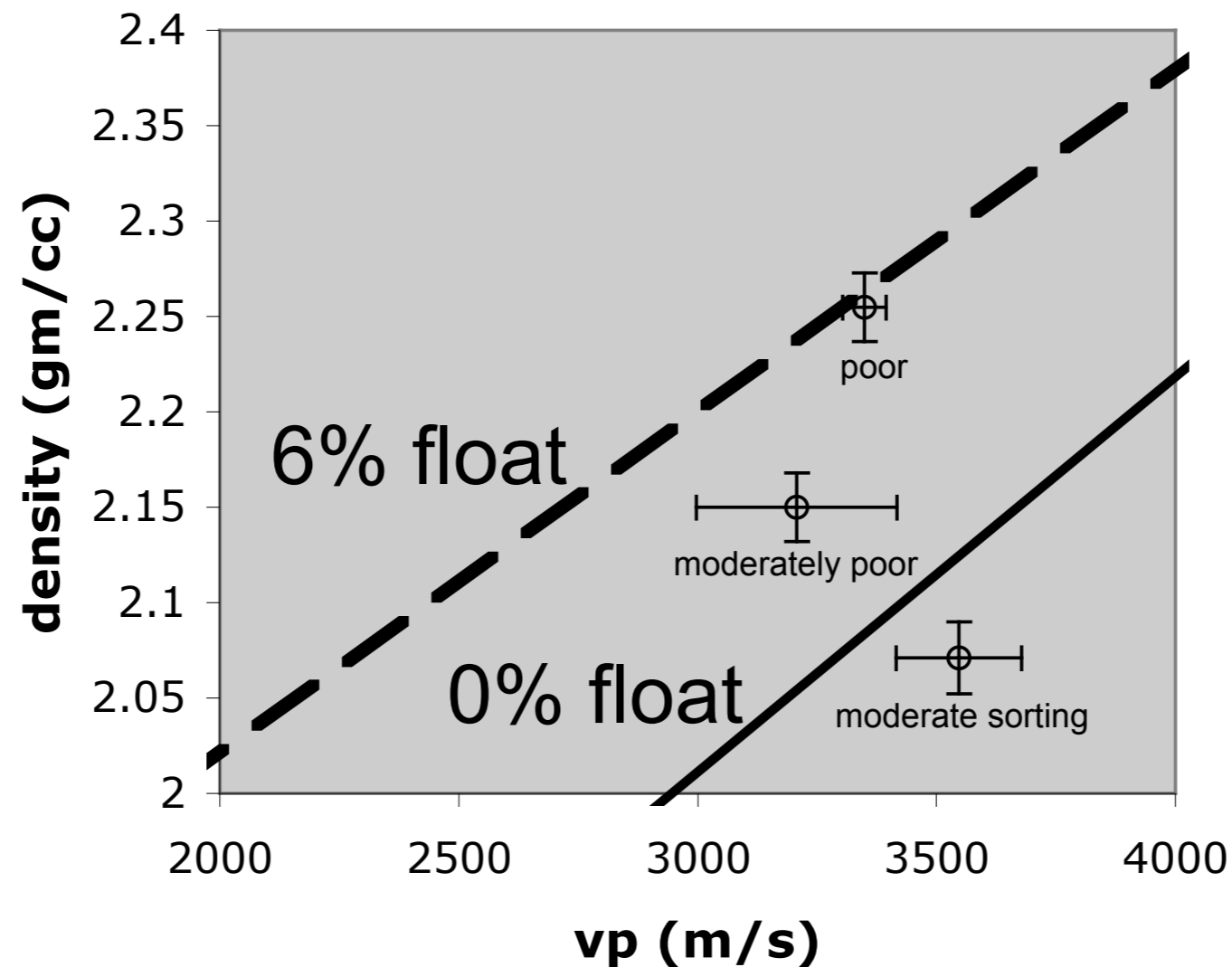
	mean	stddev	%floating
well #1	2.03	0.55	0%
well #2	1.58	0.60	3%
well #3	1.42	0.68	5%

# Good regression found between the permeability, porosity, and floating grains

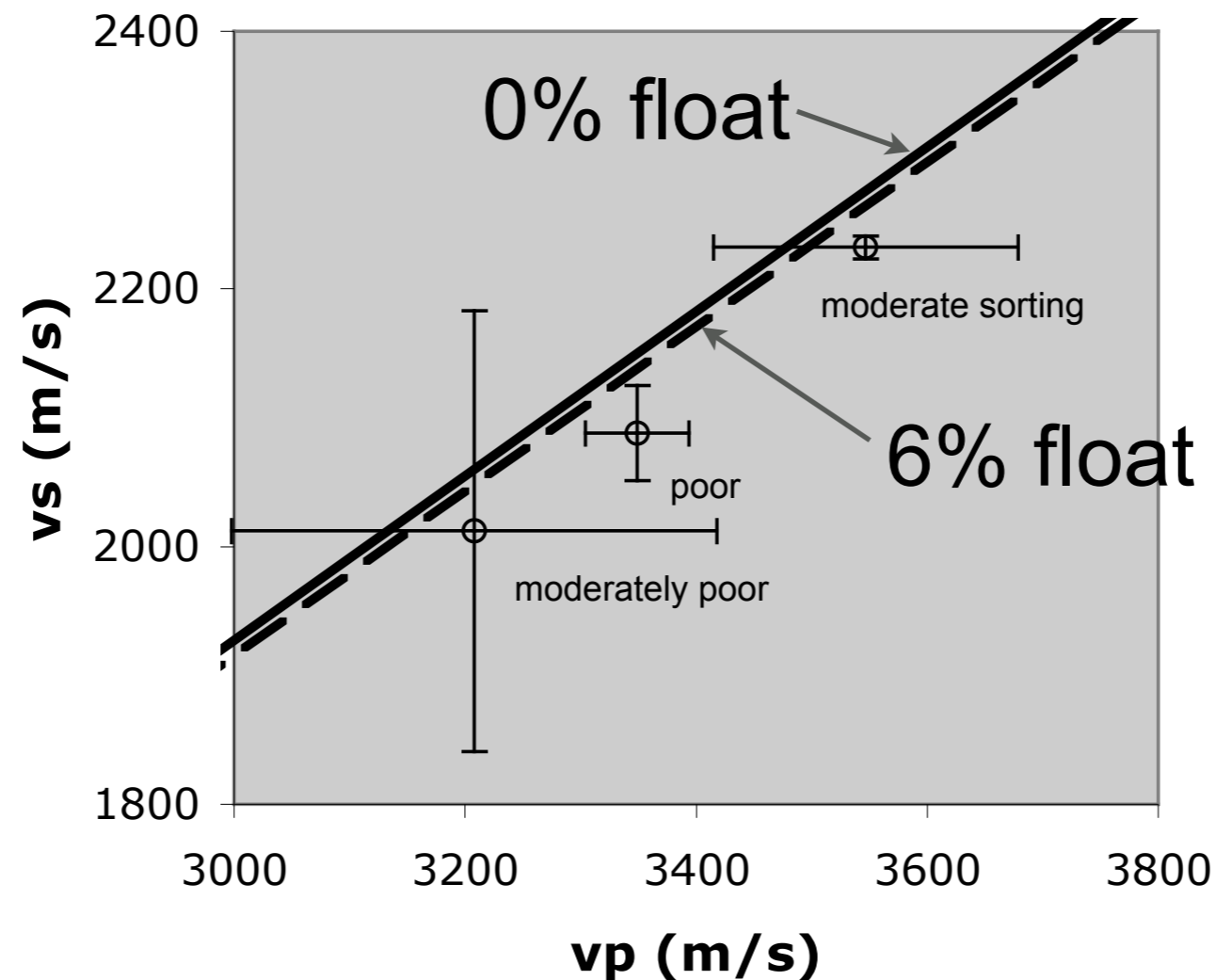


$$\log(\text{perm in mD}) = 0.198 * \text{porosity in \%} - 0.325 * \text{floating in \%} - 1.76 \quad + - 0.37$$
$$x / 2.3$$

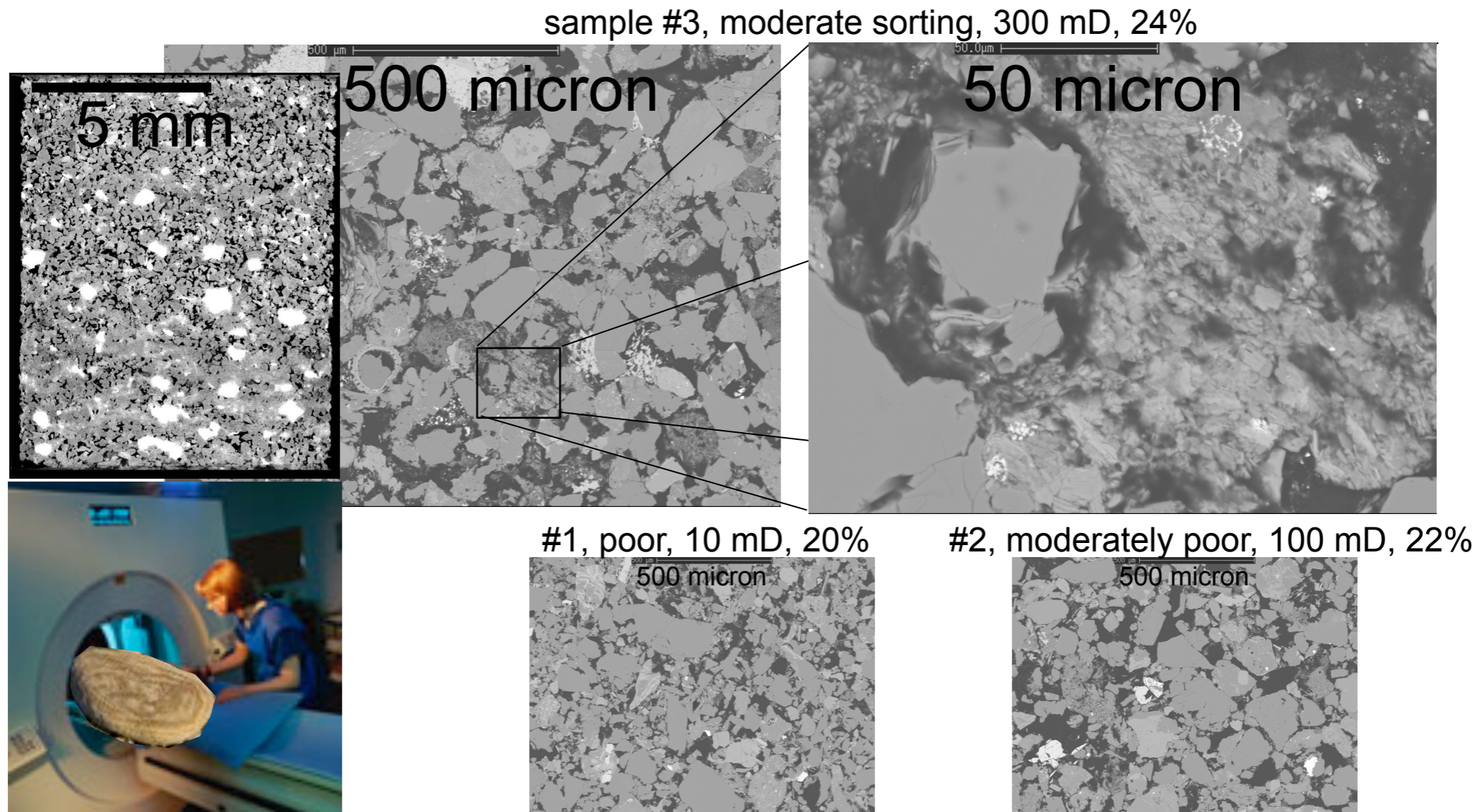
# Acoustic resonance measurements on well #2 core confirm trend seen in logs



# No change in shear velocity as seen on logs and predicted by theory



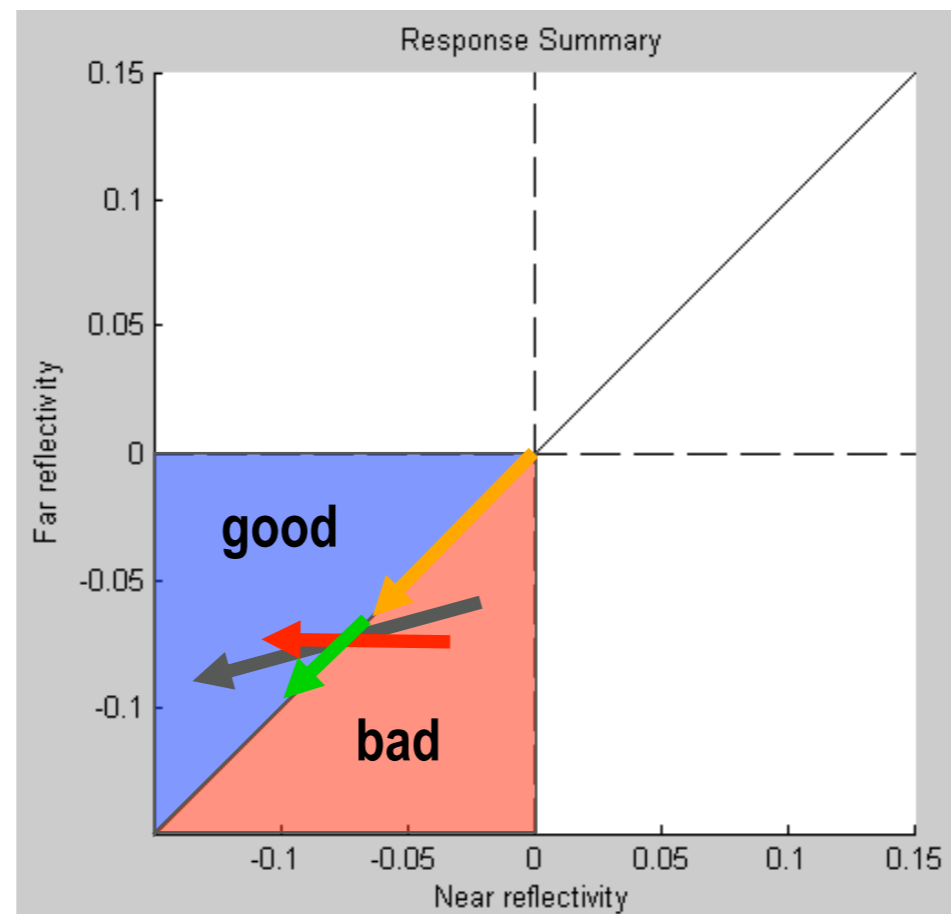
# Floating grains seen in CAT scan and SEM of well #2



# Guide to AVO interpretation

Increasing NG  
0% to 100%

Brine to Oil



Decreasing Float  
6% to 0%  
Increasing perm  
1 mD to 1000 mD

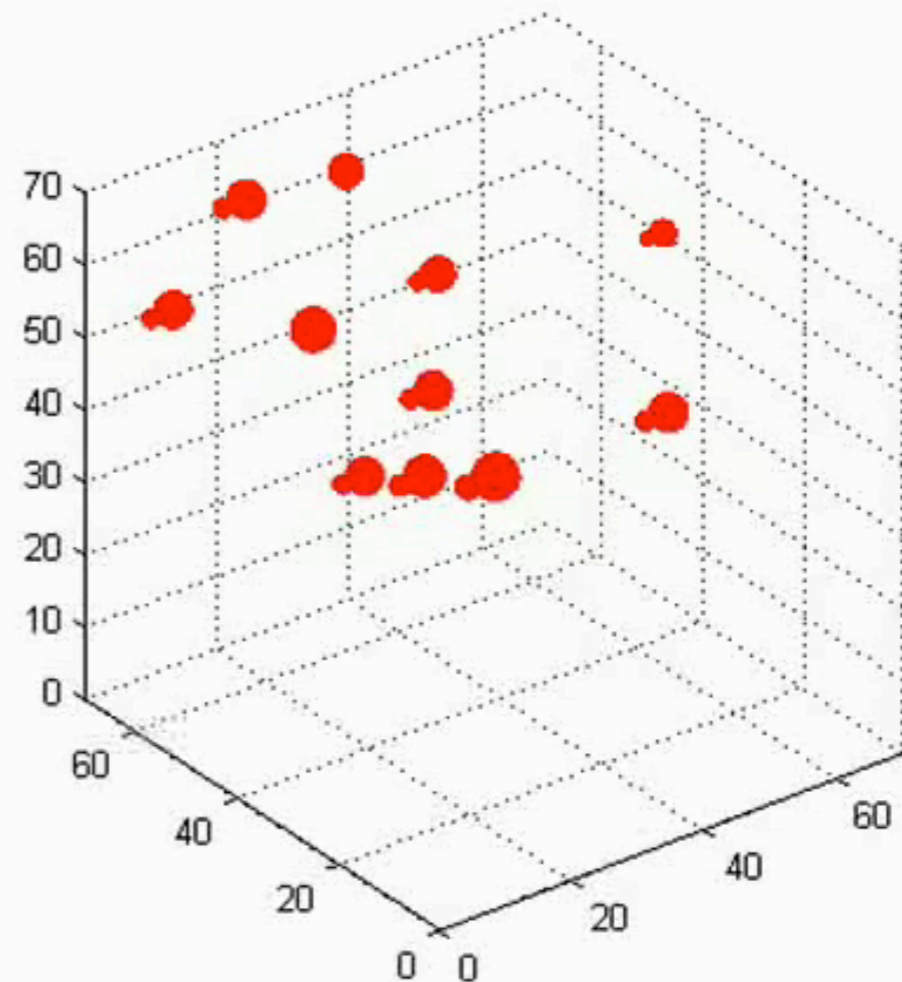


Decreasing  
Effective Stress  
1000 psi



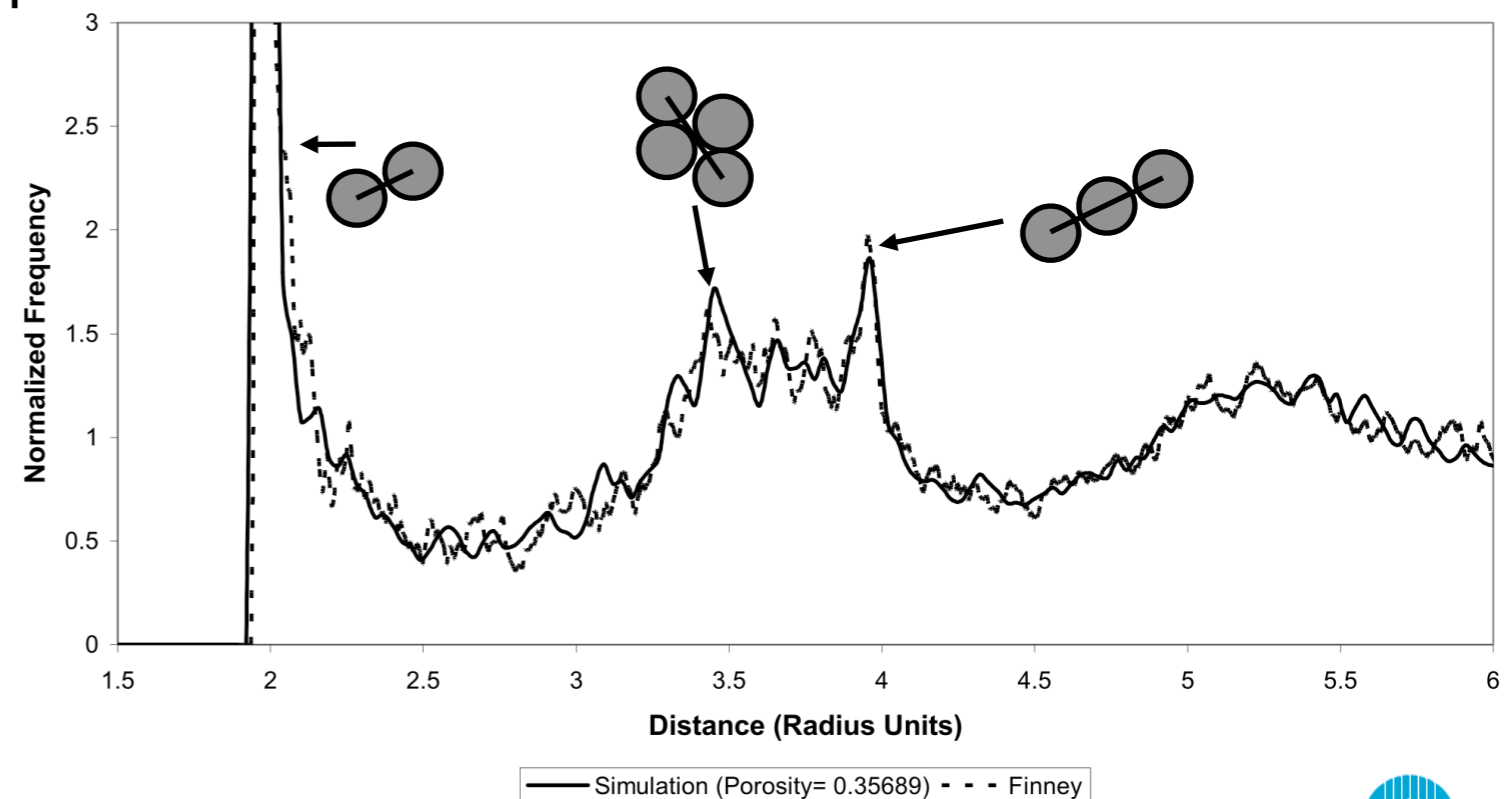
# Numerical rocks give important understanding of floating grain model

- Create sphere packings (two size) representative of unconsolidated sediment through “cooperative rearrangement” algorithm
- Quantify the number of loose grains in packings
- Understand capture fraction

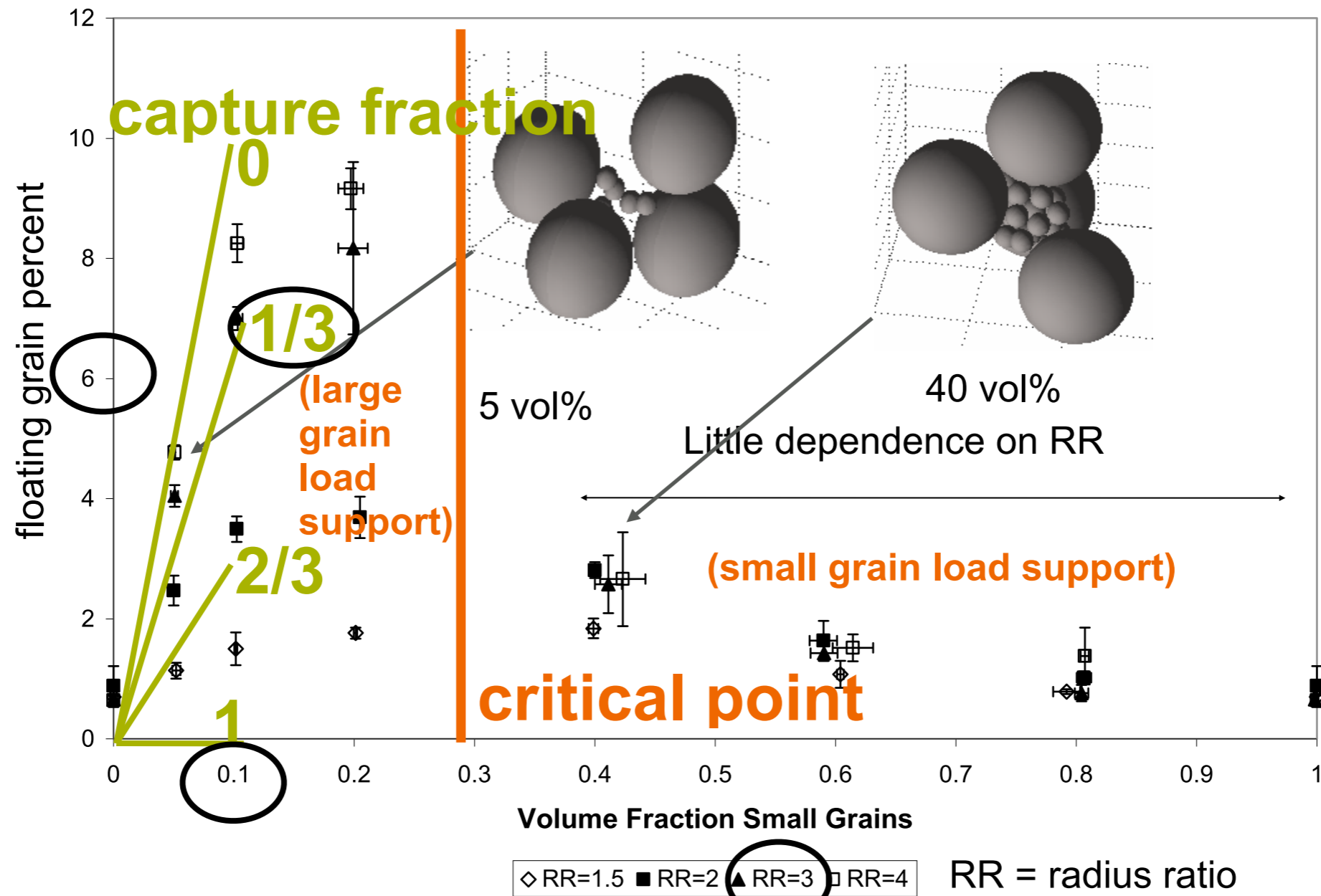


# Mono-dispersed packing validation

- Single grain size
- Comparison with Finney packing
- Quality checks:
  - Porosity
    - 36.3% Finney v. 36.2% simulation
  - Percent of loose grains
    - 1.8% Finney v. 1.6% simulation
  - Radial distribution function

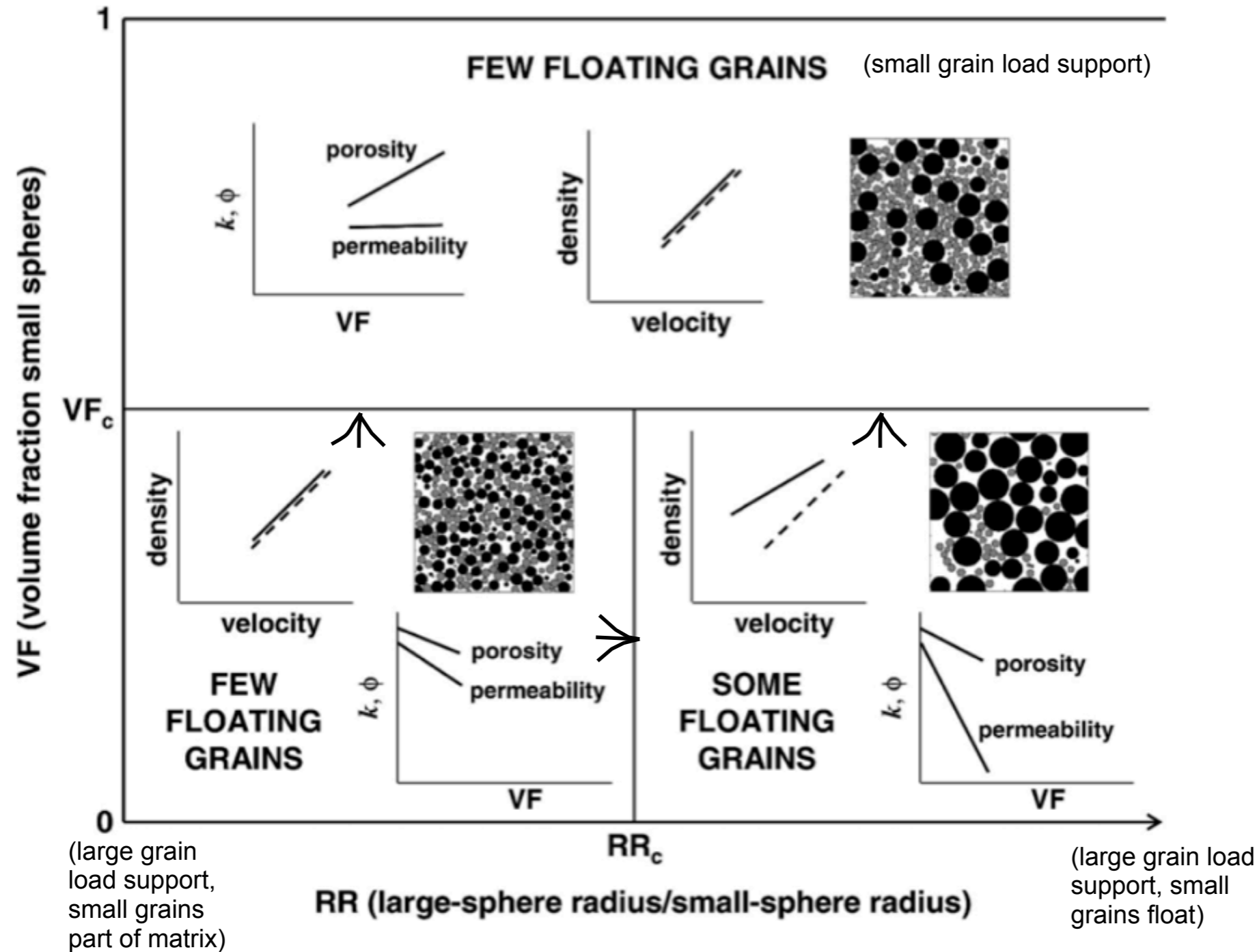


# Floating grain fraction & capture ratio demonstrated

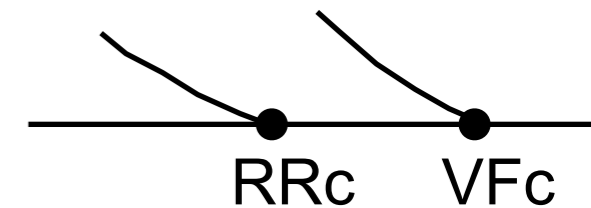


"Thermodynamics of random packing", Physics Today (June 2007)

# Phase diagram for random packing of binary mixture of spheres



note: volume fraction dominates over radius ratio critical point



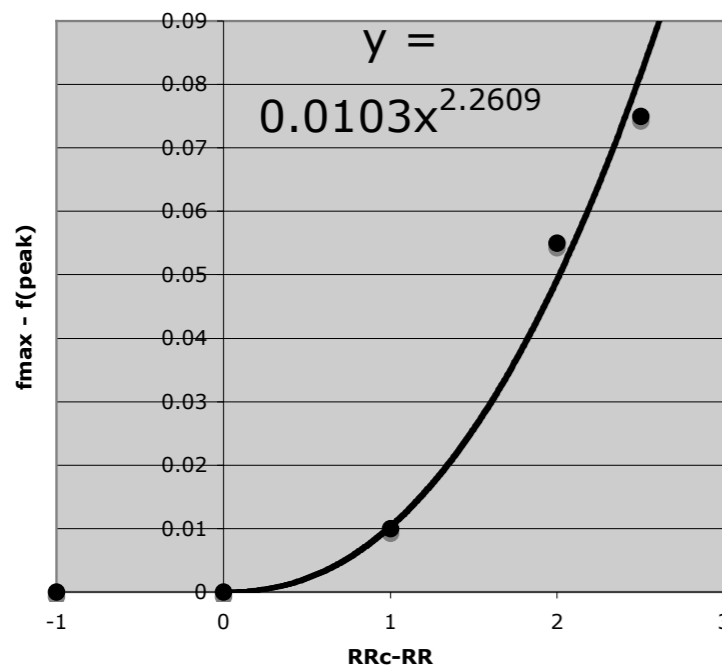
$$R_c \approx 4$$

$$VF_c \approx 0.45$$

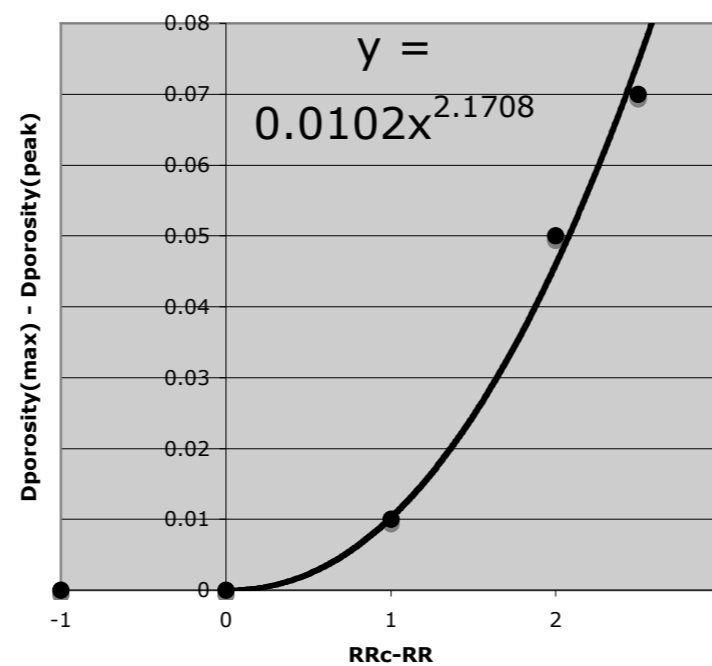
"Statistical mechanics of dense granular media", Coniglio et al., J. Cond. Matter **17**, S2557 (2005).

# Critical scaling for radius ratio critical point (RRc)

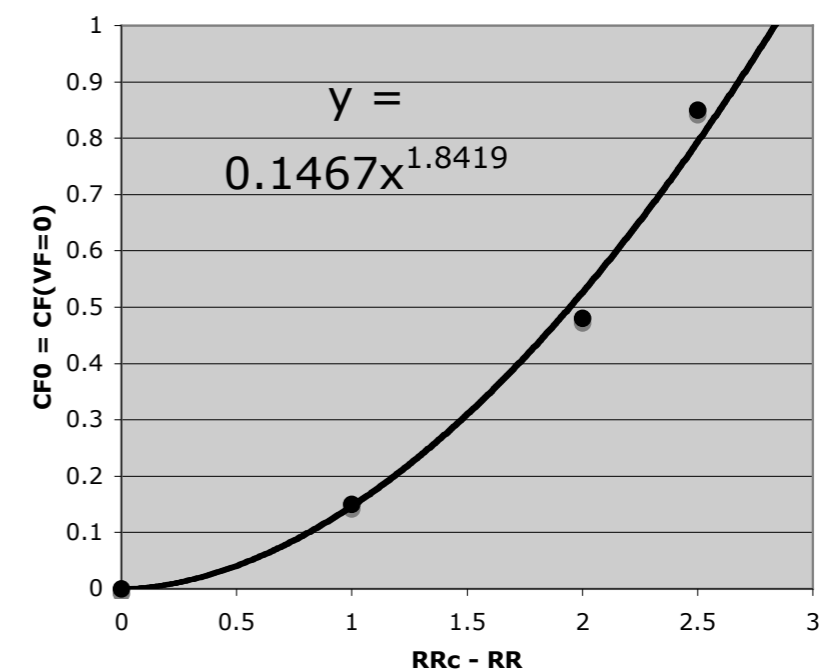
peak floating  
fraction



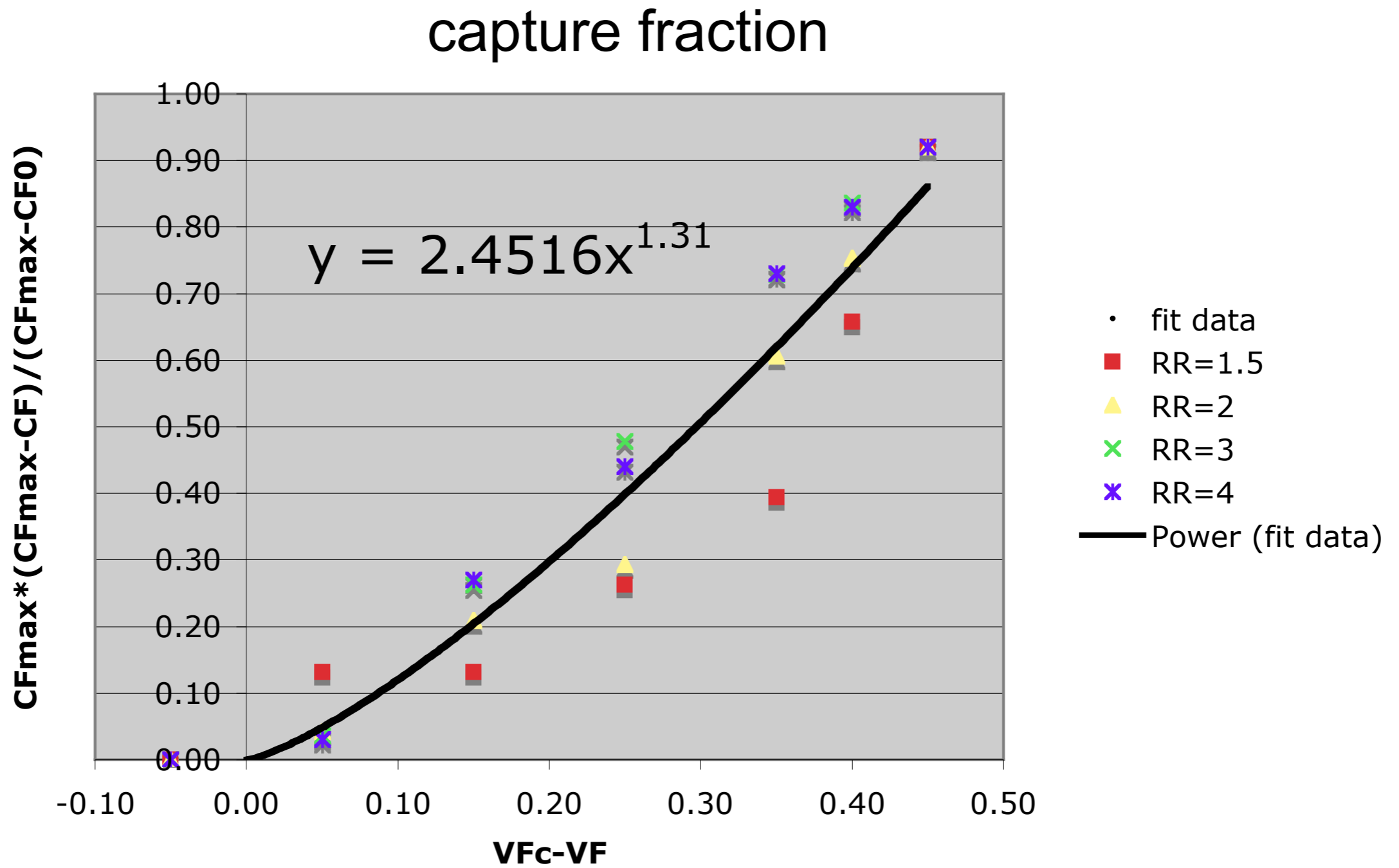
peak decrease  
in porosity



capture fraction  
@ volume  
fraction = 0

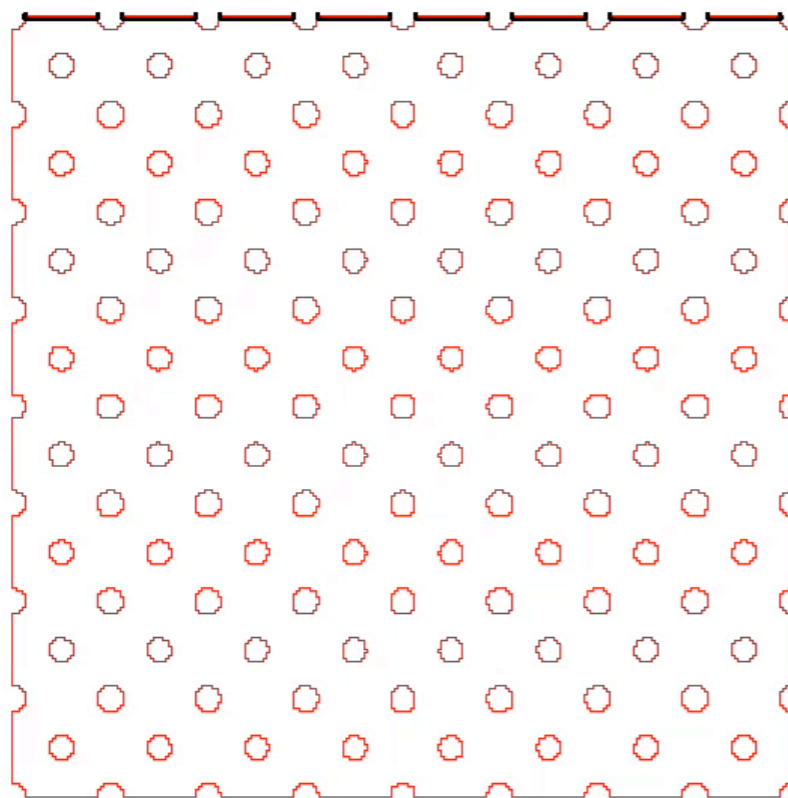


# Critical scaling for volume fraction critical point (VF<sub>c</sub>)

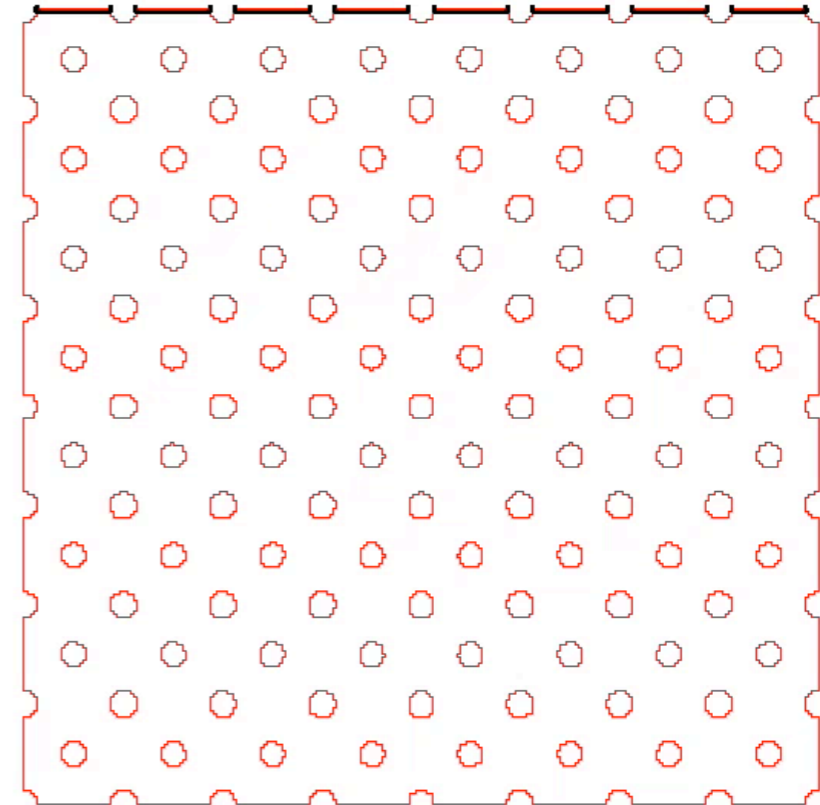


# Permeability can be simulated given 3D rock matrix from CAT

small capillary pressure



large capillary pressure

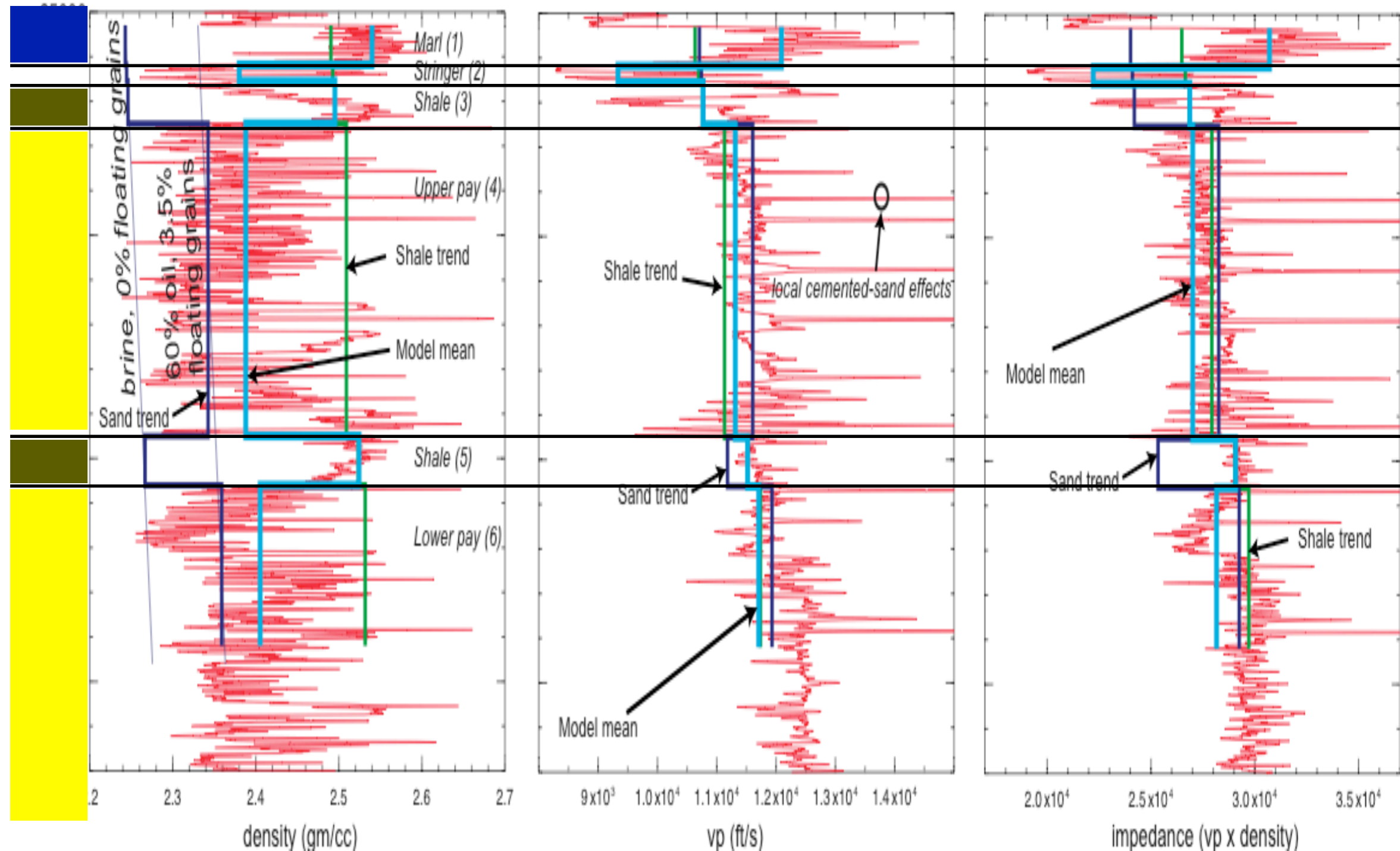


# Implementation of floating grain model in DELIVERY

$$v_p^2(\phi_{ft}, \lambda) = \frac{K_g}{\rho_g(1-\phi) + \rho_f\phi} \left( \frac{3(1-\nu)}{(1+\nu)} (1 - (\phi + \phi_{ft})/\phi_0)^\lambda + \frac{(1 - (1 - (\phi + \phi_{ft})/\phi_0)^\lambda)^2}{\phi(K_g/K_f - 1) + 1 - (1 - (\phi + \phi_{ft})/\phi_0)^\lambda} \right)$$

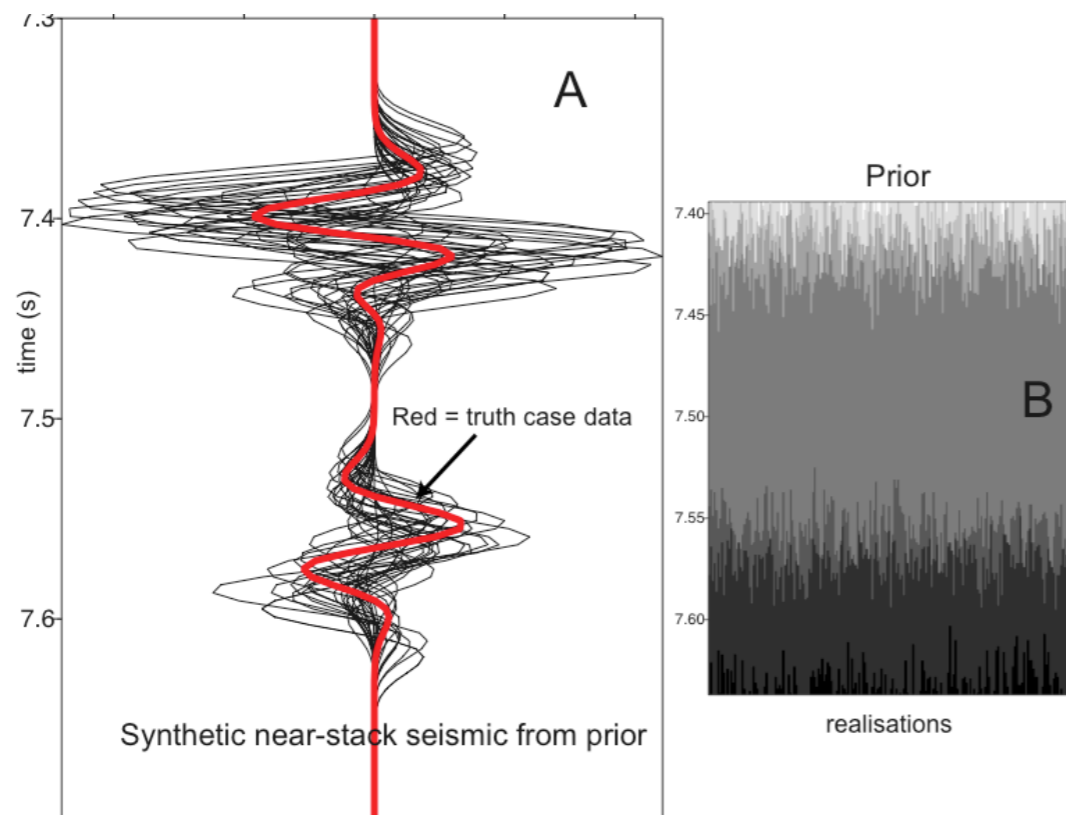
- $\phi = A_\phi + B_\phi v_p + C_\phi \phi_{flt} + \varepsilon_\phi$   
 – (from numerical inversion of above, using clusters)
- $v_p = A_p + B_p d + C_p LFIV + D_p \phi_{flt} + \varepsilon_p$   
 – (inverted from this regression, direct from log data and clusters)  
 $\phi = A' + B'd + C' \phi_{flt} + \varepsilon_\phi$ , with  $d \leftarrow (1 - \exp(-\sigma_{eff}/P_0))$   
 $C = -1/(1-f_c)$ ,  $f_c$  is 'capture fraction'
- $V_s = A_s + B_s v_p + \varepsilon_s$   
 - direct from log data

# Layer based model derived from blocking for well #2

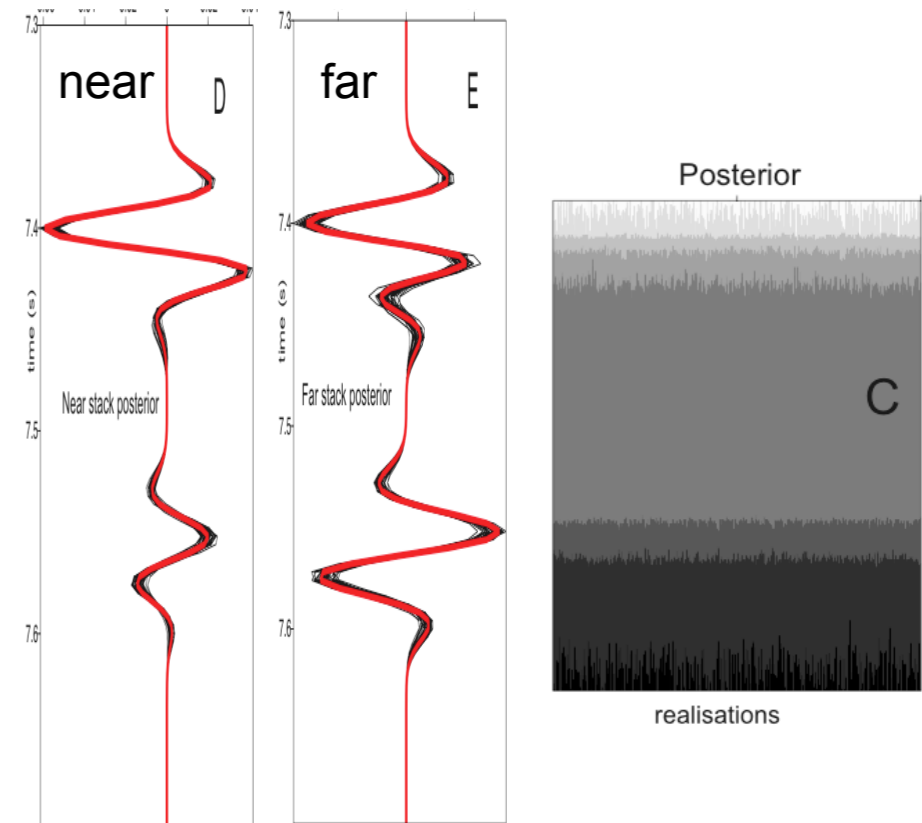


# Multiple stack inversion Bayesian inversion is used

before inversion, ignore seismic

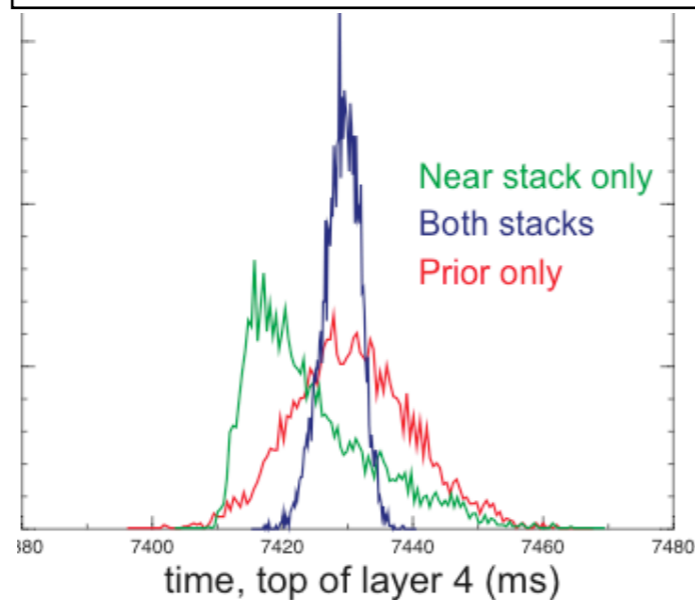


after inversion, honour seismic to within noise level

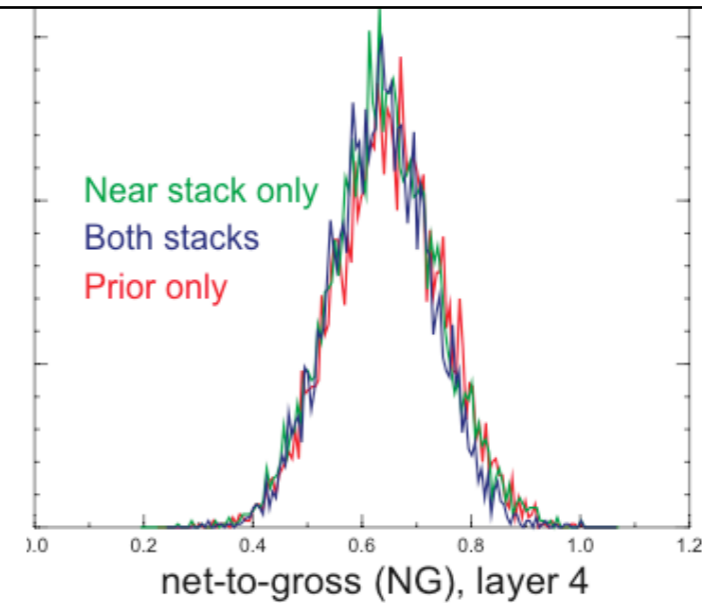


# Floating grain fraction and porosity are determined by seismic

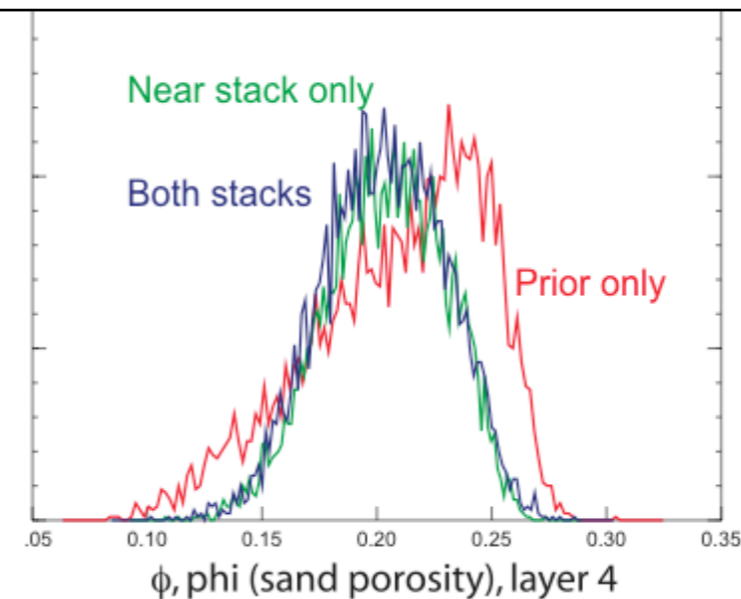
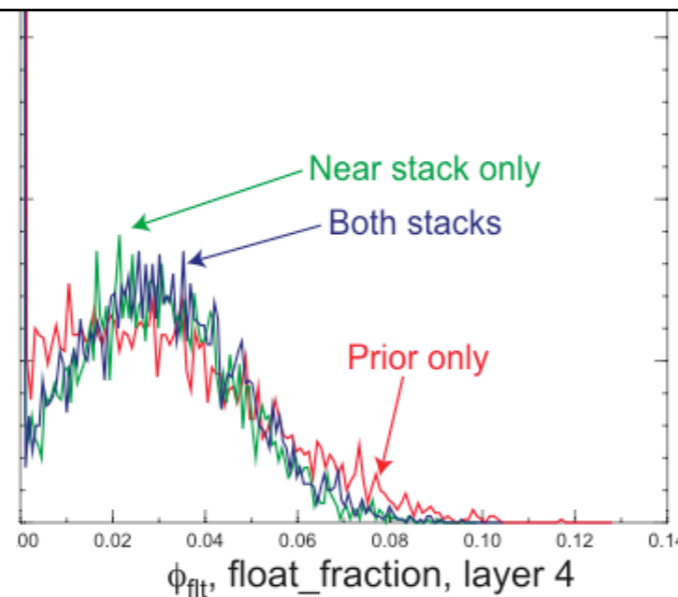
time of layer boundary - seismic determines



N/G - seismic does not determine



float fraction & porosity - seismic determines ==> permeability



# Conclusions

- **floating grain model:**
  - explains well log measurements
  - relates seismic to the sorting and the permeability
  - strong link between the microscopic picture and the mesoscopic effective media model
- **support given by:**
  - standard core measurements (laser grain size, permeability)
  - acoustical core measurements
  - CAT scan & SEM of core
  - numerical rock assembly modelling showing critical behaviour
- **practical application shown to be feasible**
  - deployed in stochastic model based inversion
  - applied to case of deepwater turbidite
  - porosity and floating grain percentage determined by seismic, **therefore permeability**

# Acknowledgments

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“A model for variation of velocity versus density trends in porous sedimentary rocks”, Demartini & Glinsky, J. Appl. Phys. **100**, 014910 (2006).

“Critical grain-size parameters for predicting framework and floating grains in sediments”, Bryant et al., J. Sedimentary Research **79**, 817 (2009).

“Detection of reservoir quality using Bayesian seismic inversion”, Gunning & Glinsky, Geophysics **72**, R37 (2007).